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ICSE Paper 2008

MATHEMATICS

SECTION A [40 MARKS]

(Answer all questions from this Section.)

Question 1.

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- (a) The simple interest on a sum of money for 2 years at 4% per annum is ₹ 340. Find :
 - (i) the sum of money and
 - (ii) the compound interest on this sum for one year payable half yearly at the same rate. [3]

(b) If
$$\frac{8a-5b}{8c-5d} = \frac{8a+5b}{8c+5d}$$
, prove that $\frac{a}{b} = \frac{c}{d}$ [3]

(c) If
$$(x-2)$$
 is a factor of $2x^3 - x^2 - px - 2$

4 (i) find the value of p.

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(ii) with the value of p, factorize the above expression completely. [4] Solution.

Given : S.I. = ₹ 340, T = 2Years, R = 4%, P = ? (a) (i)

S.I. =
$$\frac{P \times R \times T}{100}$$

P = $\frac{S.I. \times 100}{R \times T} = \frac{340 \times 100}{4 \times 2}$
= ₹4250

Ans.

(ii) Given : T = 1 Years = $1 \times 2 = 2$ times, R = 4%, $\Rightarrow R = 2\%$ (for half yearly.)

C.I. = P
$$\left[\left(1 + \frac{R}{100} \right)^{T} - 1 \right]$$

= 4250 $\left[\left(1 + \frac{2}{100} \right)^{2} - 1 \right]$
= 4250 $\left[\frac{101}{2500} \right]$ = ₹ 171.70 Ans.

(b) Given :

⇒

$$\frac{8a+5b}{8c+5d} = \frac{8a-5b}{8c-5d}$$

$$\frac{8a+5d}{8a-5b} = \frac{8c+5d}{8c-5d}$$
(Apply alternendo)
$$\frac{8a+5b+8a-5b}{8a+5b-8a+5b} = \frac{8c+5d+8c-5d}{8c+5d-8c+5d}$$
(Apply componendo and dividendo rule)
$$\frac{169}{10b} = \frac{16c}{10d}$$

$$\frac{a}{b} = \frac{c}{d}$$
Proved

Proved

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- (c) (x-2) is a factor of $2x^3 x^2 px 2$
 - (i) $\Rightarrow x = 2$ will satisfy this equation. $2 \cdot 2^3 - 2^2 - 2p - 2 = 0$ ⇒ 16 - 4 - 2p - 2 = 0 \Rightarrow 10-2p=0 $2x^2 + 3x + 1$ 2p = 10 \Rightarrow $(x-2)(2x^3-x^2-5x-2)$ $2x^3 - 4x^2$ ⇒ p = 5Ans. + (ii) On dividing $2x^3 - x^2 - 5x - 2$ by x - 2, $3x^2 - 5x - 2$ we get $3x^2 - 6x$ $(x-2)(2x^2+3x+1)$ => x-2 $(x-2)(2x^2+2x+x+1)$ ⇒ x-2(x-2)(2x(x+1)+1(x+1)) \Rightarrow (x-2)(x+1)(2x+1) \Rightarrow Ans.

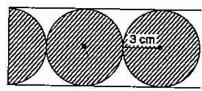
Question 2.

(a) Solve the given inequation and graph the solution on the number line.

$$y - 3 < y + 1 \le 4y + 7; y \in R.$$
 [3]

(b) In the given figure, find the area of the unshaded portion within the rectangle.

(Take $\pi = 3.14$) [3]



- (c) A shopkeeper buys a camera at a discount of 20% from the wholesaler, the printed price of the camera being ₹ 1600 and the rate of sales tax is 6%. The shopkeeper sells it to the buyer at the printed price and charges tax at the same rate. Find :
 - (i) The price at which the camera can be bought.

(ii) The VAT (Value Added Tax) paid by the shopkeeper.

[4]

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Solution.

(a) Given :
$$2y-3 < y+1 \le 4y+7, y \in \mathbb{R}$$

 $2y-3 < y+1$
 $\Rightarrow 2y-y < 3+1$
 $\Rightarrow y < 4$
solution set : $\{y \mid y \in \mathbb{R}, -2 \le y < 4\}$
 (b) Length of rectangle = 15 cm
Breadth of rectangle = 15 × 6
 $= 90 \text{ cm}^2$

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Area of circle =
$$\pi r^2$$

= $3 \cdot 14 \times 9$
= $28 \cdot 26 \text{ cm}^2$.
Area of shaded portion = Area of $2\frac{1}{2}$ circle
= $28 \cdot 26 + 28 \cdot 26 + 14 \cdot 13$
= $70 \cdot 65 \text{ cm}^2$.
Area of unshaded portion in the rectangle = Area of the rectangle
- Area of shaded portion
= $90 - 70 \cdot 65$
= $19 \cdot 35 \text{ cm}^2$ Ans.
(c) (i) Cost of camera for buyer = Printed Price + Sales tax on it
= $1600 + \frac{6}{100} \times 1600$
= $₹ 1696$ Ans.
(ii) Discount on printed price = $\frac{20}{100} \times 1600 = ₹ 320$.
Cost Price of the camera = $1600 - 320 = ₹ 1280$.
Sales tax = $\frac{6}{100} \times 1280 = ₹ 76 \cdot 80$
Tax paid by shopkeeper = $\frac{6}{100} \times 1600 = ₹ 96$.
VAT paid by shopkeeper = $96 - 76 \cdot 80$
= $₹ 19 \cdot 20$ Ans.

Question 3.

(a) David opened a Recurring Deposit Account in a bank and deposited ₹ 300 per month for two years. If he received ₹ 7725 at the time of maturity, find the rate of interest per annum.
 [3]

(b)
$$If\begin{bmatrix} 1 & 4\\ -2 & 3 \end{bmatrix} + 2M = 3\begin{bmatrix} 3 & 2\\ 0 & -3 \end{bmatrix}$$
, find the Matrix M. [3]

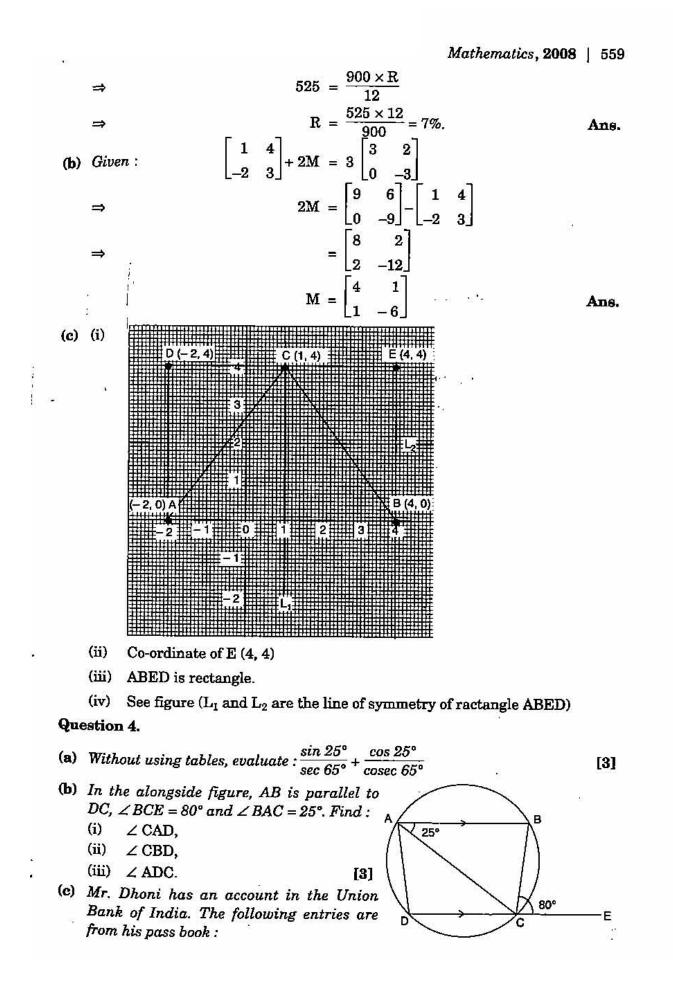
- (c) Use a graph paper for this question. (Take 1 cm = 1 unit on both the axes). Plot the points A (-2, 0), B (4, 0), C (1, 4) and D (-2, 4).
 - (i) Draw the line of symmetry of \triangle ABC. Name it L_1 .
 - (ii) Point D is reflected about the Line L_1 to get the image E. Write the coordinates of E.
 - (iii) Name the figure ABED.
 - (iv) Draw all the lines of symmetry of the figure ABED. [4]

Solution.

(a) Given : Deposited per month (P) = ₹ 300, n = 2 Year = 24 months, Amount = ₹ 7725, R = ?

Principal equivalent to 1 month =
$$P \times \frac{n(n+1)}{2} = \frac{300 \times 24 \times 25}{2}$$

= $300 \times 12 \times 25 = ₹90,000$
A = P + SI
 \Rightarrow 7725 = $24 \times 300 + \frac{90000 \times R \times 1}{12 \times 100}$



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Date	Particulars	Withdrawals (in ₹)	Deposits (in ₹)	Balance (in ₹)	
Jan 3, 07	B/F		5.04 3 1	2642.00	
Jan 16	To Self	640.00	-	2002.00	
March 5	By Cash	1 <u> </u>	850.00	2852.00	
April 10	To Self	1130.00		1722.00	
April 25	By Cheque	—	650.00	2372.00	
June 15	By Cash	577.00	2 	1795.00	

Calculate the interest from January 2007 to June 2007 at the rate of 4% per annum. [4]

Solution.

	(a)	Given :	$\frac{\sin 25^{\circ}}{\sec 65^{\circ}} + \frac{\cos 25^{\circ}}{\csc 65^{\circ}}$		
0			= sin 25° cos 65° + cos 25° sin 65°		
			$= \sin 25^\circ \cos (90^\circ - 25^\circ) + \cos 25^\circ \sin (90^\circ - 25^\circ)$		
			$= \sin 25^{\circ} \sin 25^{\circ} + \cos 25^{\circ} \cos 25^{\circ}$		24
			$= \sin^2 25^\circ + \cos^2 25^\circ = 1 \qquad (:: \sin^2 \theta + \cos^2 \theta =$	= 1) Ans.	33
	(b)	(i)	$\angle BCE = \angle BAD = 80^{\circ}$		35
			('.' ext. of cyclic quad. is equal to opp. in	it. angle.)	- 2
		⇒	$\angle CAD = \angle BAD - \angle BAC = 80^\circ - 25^\circ = 55^\circ$	Ans.	
		(ii)	$\angle CBD = \angle CAD$ ("." Angle of the same segment ar		
			= 55°	Ans.	
		(iii)	AB DC (given)		
			$\angle BAD + \angle ADC = 180^{\circ}$		
		⇒	$(25 + 55) + \angle ADC = 180^{\circ}$		88 14
			$= 180 - 80 = 100^{\circ}$ (: ABCD is cycl	ic quad.)	
	(-)			Ans.	
	(c)	94	Minimum Balance for January = ₹ 2,002		03
		2	Minimum Balance for February = ₹ 2,002 Minimum Balance for March = ₹ 2.852		
			Minimum Balance for March $= ₹$ 2,852 Minimum Balance for April $= ₹$ 1,722		各
			Minimum Balance for May \approx ₹ 2,372		45
			Minimum Balance for June = ₹ 1,795		
			Total = ₹ 12,745		
			S.I. = $\frac{\mathbf{P} \times \mathbf{R} \times \mathbf{T}}{100}$		
				55	
			$=\frac{12745\times4\times1}{100\times12}$		
			= ₹42.48	Ans.	
					6



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SECTION B [40 Marks]

Answer any Four Questions in this Section.

Question 5.

(a) A function in x is defined as : *

$$f(x) = \frac{x+2}{2x-1}; x \in R \text{ and } x \neq \frac{1}{2},$$

Find: (i) $f(-3),$
(ii) $f(x-1),$
(iii) $x \text{ if } f(x) = 1.$ [3]

(b) Prove the identity:
$$\frac{\sin A}{1 + \cos A} = \operatorname{cosec} A - \cot A.$$
 [3]

(ii) In what ratio is the line joining AB, divided by the x-axis? [4] Solution.

(b)

 \Rightarrow

L.H.S. =
$$\frac{\sin A}{1 + \cos A}$$

= $\frac{\sin A}{1 + \cos A} \times \frac{1 - \cos A}{1 - \cos A}$
= $\frac{\sin A (1 - \cos A)}{1 - \cos^2 A}$
= $\frac{\sin A (1 - \cos A)}{\sin^2 A}$
= $\frac{1}{\sin A} - \frac{\cos A}{\sin A}$
= $\cos ec A - \cot A = R.H.S.$

1

Proved

Ans.

(c) (i) Given : A = (-4, 3), B = (8, -6)

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

= $\sqrt{(8 + 4)^2 + (-6 - 3)^2}$
= $\sqrt{144 + 81}$
= $\sqrt{225} = 15.$

2

(ii) Let any point on x-axis will be P(x, 0).

$$x = \frac{mx_1 + nx_2}{m + n},$$

$$y = \frac{my_1 + ny_2}{m + n}$$

$$0 = \frac{m \cdot 3 + n \cdot (-6)}{m + n}$$

$$\Rightarrow \quad 3m = 6n$$

$$\Rightarrow \qquad \frac{m}{n} = \frac{6}{3} = \frac{2}{1}$$

The ratio will be 2 : 1.

Ans.



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Question 6.

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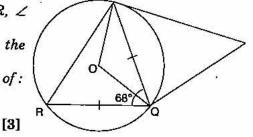
(a) Solve the following quadratic equation for x and give your answer correct to two decimal places :

5x(x+2) = 3

(b) In the figure given alongside
$$PQ = QR$$
, \angle
 $RQP = 68^\circ$, PC and CQ are tangents to the

circle with centre O. Calculate the values of :

- (i) $\angle QOP$,
- (ii) $\angle QCP$.



- (c) A company with 4000 shares of nominal value of ₹ 110 each declares an annual dividend of 15%. Calculate :
 - (i) The total amount of dividend paid by the company.
 - (ii) The annual income of Shah Rukh who holds 88 shares in the company.
 - (iii) If he received only 10% on his investment, find the price Shah Rukh paid for each share.

Solution.

(a) Given :

Hence

$$5x (x + 2) = 3$$

$$5x^2 + 10x - 3 = 0$$

Camparing with $ax^2 + bx + c = 0$, we get a = 5, b = 10 and c = -3.

We know that

$$x = \frac{2a}{2a}$$

$$= \frac{-10 \pm \sqrt{(10)^2 - 4 \times 5 \times (-3)}}{2 \times 5}$$

$$= \frac{-10 \pm \sqrt{100 + 60}}{10}$$

$$= \frac{-10 \pm 4 \sqrt{10}}{10} = \frac{-5 \pm 2 \sqrt{10}}{5}$$

$$= \frac{-5 \pm 2 \times 3 \cdot 16}{5} = \frac{-5 \pm 6 \cdot 32}{5}$$

$$x = 0.26 \text{ or } -2.26.$$

 $-b \pm \sqrt{b^2 - 4ac}$

Ans.

[3]

(b) Given : $PQ = QR, \angle RQP = 68^{\circ}$ (i) In \triangle PQR, PQ = RQ $\angle PRQ = \angle QPR$ $\angle PRQ + \angle QPR + 68^\circ = 180^\circ$ ⇒ [sum of the angle of a \triangle is 180°] \Rightarrow $2 \angle PRQ = 180 - 68 = 112^{\circ}$ $\angle PRQ = 56^{\circ}$ ⇒ $\angle QOP = 2 \times \angle PRQ$ [angle at centre of the circle is twice the angle of at the remaining circumference] $= 2 \times 56 = 112^{\circ}$ Ans.

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	(ii) ∠	PQC	$= \angle PRQ$				
	A.	2001	$= \angle PRQ$				
			$= \angle QPC = 56^{\circ}$				
	$\Rightarrow \angle PQC + \angle QPC + QPC + \angle QPC + A QP$						
	$\Rightarrow 56^\circ + 56^\circ + \angle$	있는 것이야???					
	⇒ Z	QCP	$= 180^{\circ} - 56^{\circ} - 56^{\circ}$ $= 68^{\circ}$	4-1-0			
	Given Ma afaharan - 4000 N	Ans.					
(c)	Given : No. of shares = 4000, NV = ₹ 110, Dividend = 15%						
	(i) Dividend or	n 1 sh	$are = \frac{15}{100} \times 110$				
			= ₹ 16-50				
	Total	divid	$end = 4000 \times 16.50$				
	(**))0 ~h.	= ₹66000	Ans.			
	(ii) Income on 8	oo sha	ares = 88×16.50 = $\mathbf{\overline{1}},452$				
	Annual income of Sh	oh R		Ans.			
	(iii) Let his inv			11115			
				13			
		100	x = 1452				
			x = ₹14520				
	Price for ea	ich sh	are $=\frac{14520}{88} = ₹ 165.$	Ans.			
Que	estion 7.			10			
(a)	The income of Mr. Bachhan wa	s as f	ollows : **				
	Basic Salary		: ₹20,000 per month				
	 Dearness Allowance 		: < 12,000 per month	<u>.</u>			
	• Interest from Bank		: 💐 16,000 for the whole ye	ar.			
	Savings : • Contribution towards Provid	Jan+ I	Fund . 15% of Paolo calan				
	 Contribution towards Frond National Savings Certificate 		: ₹40,000				
	 Contribution towards LIC p. 						
	Donations		n an				
			🕇 12,000 (eligible for 100% exemp				
			every month towards Income to				
	그 수지	- T	year, calculate the tax Mr. Bach	han has to [6]			
	pay in the last month of the find	ancia	i year:	[0]			
	Tax slab:		NT- d				
	Upto < 1,00,000	2	No tax.	00.000			
	From < 1,00,001 to < 1,50,000		10% of the income exceeding < 1	10			
	From ₹ 1,50,001 to ₹ 2,50,000	30	₹ 5,000+ 20% of the income ₹ 1,50,000	exceeding			
	Above ₹ 2,50,000	:	₹ 25,000 + 30% of the income ₹ 2,50,000	exceeding			
	Deductions against savings	8	Upto a maximum amount of ₹	1,00,000			
	Education Cess	5	2% of the tax payable.				

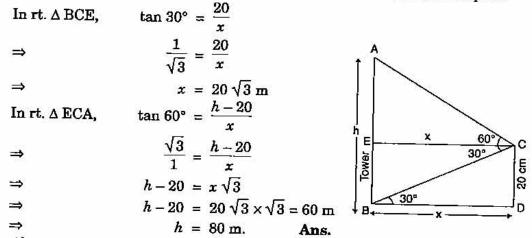
**. Solution has not given due to out of present syllabus.



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- (b) A vertical pole and a vertical tower are on the same level ground. From the top of the pole the angle of elevation of the top of the tower is 60° and the angle of depression of the foot of the tower is 30°. Find the height of the tower if the height of the pole is 20 m.

Solution.

(b) Let h be the height of tower and x be the distance between tower and pole.



Question 8.

(a) Find the H.C.F. of the given polynomials : **

$$x^2 - \frac{1}{a^2}$$
 and $x^2 + \frac{2x}{a} + \frac{1}{a^2}$ [3]

- (b) Using a ruler and a pair of compasses only, construct :
 - (i) A triangle ABC, given AB = 4 cm, BC = 6 cm and $\angle ABC = 90^\circ$.
 - (ii) A circle which passes through the points A, B and C and mark its centre as
 O.
- (c) Points A and B have coordinates (7, -3) and (1, 9) respectively. Find :
 - (i) The slope of AB.
 - (ii) The equation of the perpendicular bisector of the line segment AB.
 - (iii) The value of 'p' if (-2, p) lies on it.

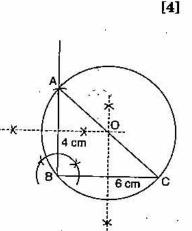
Solution.

(b) Steps of Construction :

- (1) Draw side BAC, 6 cm.
- (2) Draw a $\angle B = 90^\circ$, and cut AB = 4 cm.

(3) Meet AC.

- (4) Draw Bisector of BC and AB. Which meet at point 'O'.
- (5) Now draw a circle as centre 'O'.
- (6) This circle passes through the point A, B, and 'C'.



^{**} Solution has not given due to out of present syllabus.



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(c) (i) Slope of AB
$$(m_1) = \frac{y_2 - y_1}{x_2 - x_1}$$

 $= \frac{9+3}{1-7} = \frac{12}{-6} = -2$ Ans. A $\frac{(7, -3)}{(7, -3)} = \frac{P_{(-2, p)}}{D} = (1, 9)$
(ii) The mid point of line AB $= (\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2})$
 $= (\frac{7+1}{2}, \frac{-3+9}{2}) = (4, 3)$

Slope of perpendicular bisector of AB

$$m_2 = \frac{-1}{m_1} = \frac{-1}{-2} = \frac{1}{2}$$

Equation of perpendicular bisector

 $y - y_1 = m (x - x_1)$ $\Rightarrow \qquad y - 3 = \frac{1}{2}(x - 4)$ $\Rightarrow \qquad 2y - 6 = x - 4$ $\Rightarrow \qquad x - 2y + 2 = 0$

(iii) Given point (-2, p) lies on the equation x - 2y + 2 = 0

$$\begin{array}{ccc} -2-2p+2 &= 0\\ \Rightarrow & -2p &= 0\\ \Rightarrow & p &= 0 \end{array}$$
 Ans.

Question 9.

(a) Given
$$A = \begin{bmatrix} p & 0 \\ 0 & 2 \end{bmatrix}$$
, $B = \begin{bmatrix} 0 & -q \\ 1 & 0 \end{bmatrix}$, $C = \begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix}$ and $BA = C^2$.

Find the values of p and q.

- (b) In ∆ ABC, AP : PB = 2 : 3. PO is parallel to BC and is extended to Q so that CQ is parallel to BA. Find :
 - (i) Area $\triangle APO$: area $\triangle ABC$.
- (ii) Area $\triangle APO$: area $\triangle CQO$.
- (c) The volume of a conical tent is 1232 m³ and the area of the bare floor is 154 m²: ^B Calculate the :
 - (i) Radius of the floor.

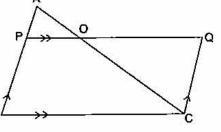
(ii) Height of the tent.

(iii) Length of the canvas required to cover this conical tent if its width is 2 m.

[3]

Solution.

(a) Given : A =
$$\begin{bmatrix} p & 0 \\ 0 & 2 \end{bmatrix}$$
, B = $\begin{bmatrix} 0 & -q \\ 1 & 0 \end{bmatrix}$, C = $\begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix}$
BA = C²



Ans.

[3]

[4]

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566 | ICSE Last 10 Years Solved Papers $\begin{bmatrix} 0 & -q \\ 1 & 0 \end{bmatrix} \begin{bmatrix} p & 0 \\ 0 & 2 \end{bmatrix} = \begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} 2 & -2 \\ 2 & 2 \end{bmatrix}$ p = 8, q = 4 $\frac{AP}{PB} = \frac{2}{3} = \frac{AO}{OC}$ Ans. \Rightarrow **(b)** (i) $\frac{AP}{AP + PB} = \frac{2}{2+3}$ $\frac{AP}{AB} = \frac{2}{5}$...(1) ⇒ PO is parallel to BC and CQ is parallel to BA. So, PBCQ is a parallelogram. PB = CQ⇒ $\frac{AP}{PB} = \frac{2}{3} = \frac{AP}{CQ}$ ⇒ In \triangle APO and \triangle ABC, $\angle APO = \angle ABC$ (∵ PO || BC) $\angle A = \angle A$ $\triangle APO \sim \triangle ABC$ ⇒ $\frac{AP}{AB} = \frac{AO}{AC} =$ 25 AP² area of \triangle APO $\frac{1}{\text{area of } \Delta \text{ ABC}} = \frac{A}{AB^2}$ 1 ⇒ [Ratio between the areas of two similar Δ 's is equal to the ratio between the squares of their corresponding sides] $=\left(\frac{2}{5}\right)^{2}=\frac{4}{25}$ Ans. (ii) In \triangle APO and \triangle CQO, $\angle AOP = \angle COQ$ (vertically opp.) $\angle OAP = \angle OCQ$ $\triangle AOP \sim \triangle COQ$ (By A.A axiom) \Rightarrow $\frac{\text{area of } \Delta \text{ APO}}{\text{area of } \Delta \text{ CQO}} = \frac{\text{AP}^2}{\text{CQ}^2} = \left(\frac{2}{3}\right)^2 = \frac{4}{9}$ Ans. So (c) Given : Volume (V) = 1232 m, Area of base = 154 m^2 Let r be the radius and h be the height. Area = $\pi r^2 = 154$ (i) $\frac{22}{7}r^2 = 154$ $r^2 = 49$ $r = 7 \,\mathrm{m}$ Ans. Volume (V) = $\frac{1}{3}\pi r^2 h = 1232$ (ii) $\frac{1}{3} \times \frac{22}{7} \times (7)^2 \times h = 1232$

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$$h = \frac{1232 \times 3}{22 \times 7} = 24 \text{ m.}$$
 Ans.

(iii) Let l be the slant height of the conical tent, then

$$l = \sqrt{h^2 + r^2} = \sqrt{24^2 + 7^2} = 25m$$
Area of canvas required = Curved surface area of the tent

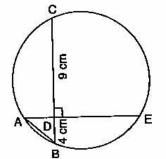
$$\Rightarrow \text{ Length } \times \text{ width of canvas } = \pi rl \text{ (for tent)}$$

$$\Rightarrow \text{ Length of canvas } \times 2 = \frac{22}{7} \times 7 \times 25$$
Length of canvas = $\frac{550}{2} = 275 \text{ m.}$
Ans

Question 10.

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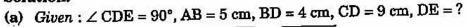
(a) In the given figure, AE and BC intersect each other at point D. If $\angle CDE = 90^{\circ}$, [3] AB = 5 cm, BD = 4 cm and CD = 9 cm, find DE.



- (b) A straight line AB is 8 cm long. Locate by construction the locus of a point. which is :
 - (i) Equidistant from A and B.
 - (ii) Always 4 cm from the line AB.
 - (iii) Mark two points X and Y, which are 4 cm from AB and equidistant from A [8] and B, Name the figure AXBY.
- (c) Some students planned a picnic. The budget for the food was ₹ 480. As eight of
 - them failed to join the party, the cost of the food for each member increased by $extsf{R}$ [4] 10. Find how many students went for the picnic.

Solution.

⇒



$$AD = \sqrt{AB^2 - DB^2} = \sqrt{25 - 16} = 3$$

$$DA \times DE = DB \times DC$$
 (Product of the length of their segment is equal.)
 $3 \times DE = 4 \times 9$

Ans.

B

P

x

0

0

B cm

DE = 12 cm=>

(b) Steps of Construction :

- Draw AB is 8 cm, Draw PQ the perpen-dicular bisector (i) of AB.
- (ii) Draw CD and EF both parallel to AB and each at a distance of 4 cm from AB.

(iii) AXBY is a square.

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- (c) Let the no. of students planned a picnic = x.
 - Budget for food = ₹480Budget for each student = $\frac{480}{x}$

If eight student failed to join the party, the cost for each student $=\frac{480}{x-8}$

	480 480
	$\frac{1}{x-8}-\frac{1}{x}=10$
	$\frac{480x - 480(x - 8)}{r(x - 8)} = 10$
	- (0)
⇒	480 x - 480 x + 3840
14-13.0	x(x-8) = 10
₽	$x^2 - 8x - 384 = 0$
⇒	$x^2 - 24x + 16x - 384 = 0$
	x(x-24)+16(x-24) = 0
⇒	(x-24)(x+16) = 0
⇒	x = 24, -16
But the r	\sim - 23, - 10 number of students can not be possible

$$x = 24$$

:. The number of student who went for picnic = x - 8 = 24 - 8 = 16 Ans.

Question 11.

(a) The weight of 50 apples were recorded as given below. Calculate the mean weight, to the nearest gram, by the Step Deviation Method.
 [5]

Weight in grams	80-85	DE OO	00.05		C		(V)
	00-00	00-90	90-95	95-100	100-105	105-110	110_115
No. of apples	5	8	10	12	0		110-110
I lois 1	and the second		/		•	4	37

(b) Using a graph paper, draw an ogive for the following distribution which shows the marks obtained in the General Knowledge paper by 100 students.

1/2/2/ 1/23	0-10	10-20	20-30	30-40	40-50	50-60	6070	70-80
No. of students		10	20	25	15	12	0	10-00
Use the ogive to	estimate			<u></u>		12		4

(i) The median.

(ii) The number of students who score marks above 65.

Solution.

(a) Weight No. of apples Mid Value $u_i = \frac{x - A}{C}$ $f_i u_i$ (f.) (x)80-85 5 82.5 -3 -1585-90 8 87.5 -2-1690-95 10 92.5 -1 -10 95-100 12 97.5 0 0 100-105 8 102.5 1 8 105-110 4 107.5 2 8 110-115 3 112.53 9 $\Sigma f_i = 50$ $\Sigma f_i u_i = -16$

[5]



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