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# CBSE 12th Mathematics 2014 Unsolved Paper <br> Outside Delhi 

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# CBSE 12th Mathematics 2014 Unsolved Paper Outside Delhi <br> TIME - 3HR. QUESTIONS - 26 

## THE MARKS ARE MENTIONED ON EACH QUESTION

SECTION - A
Q.1. If $(R)=\{(x, y): x+2 y=8\}$ is a relation on $N$, write the range of $R$.
Q.2. If

$$
\tan ^{-1} x+\tan ^{-1} y=\frac{\pi}{4}, x y<1
$$

Then write the value of $\boldsymbol{x}+\boldsymbol{y}+\boldsymbol{x} \boldsymbol{y}$. I mark
Q.3. If $\mathbf{A}$ is a square matrix such that $A^{2}=A$, then write the value of $7 A-(I+A)^{3}$, where $I$ is an identity matrix. 1 mark
Q.4. If $\left[\begin{array}{cc}x-y & z \\ 2 x-y & w\end{array}\right]=\left[\begin{array}{cc}-1 & 4 \\ 0 & 5\end{array}\right]$, find the value of $\boldsymbol{x}+\boldsymbol{y}$. 1 marks
Q.5. If $\left|\begin{array}{cc}3 x & 7 \\ -2 & 4\end{array}\right|=\left|\begin{array}{ll}8 & 7 \\ 6 & 4\end{array}\right|$, find the value of $x$. I mark
Q.6. If $f(x)=\int_{0}^{\boldsymbol{x}} \boldsymbol{t} \sin \boldsymbol{t} d \boldsymbol{t}$, then write the value of $\boldsymbol{f}^{\prime}(x)$. \$inark
Q.7. Evaluate: mark

$$
\int_{2}^{4} \frac{x}{x^{2}+1} d x
$$

Q.8. Find the value of ' $p$ ' for which the vectors $3 \hat{\imath}+2 \widehat{\jmath}+9 \widehat{k}$ and $\widehat{\imath}-2 p \widehat{\jmath}+3 \widehat{k}$ are parallel.
Q.9. Find $\overrightarrow{\boldsymbol{a}} .(\overrightarrow{\boldsymbol{b}} \times \overrightarrow{\boldsymbol{c}})$, if $\overrightarrow{\boldsymbol{a}}=\mathbf{2} \widehat{\boldsymbol{\imath}}+\widehat{\boldsymbol{\jmath}}+3 \widehat{\boldsymbol{k}}, \overrightarrow{\boldsymbol{b}}=-\widehat{\boldsymbol{\imath}}+\mathbf{2} \widehat{\boldsymbol{\jmath}}+\widehat{\boldsymbol{k}}$ and $\overrightarrow{\boldsymbol{c}}=\mathbf{3} \widehat{\boldsymbol{\imath}}+\widehat{\boldsymbol{\jmath}}+2 \widehat{\boldsymbol{k}}$ mark
Q.10. If the Cartesian equation of a line are

$$
\frac{3-x}{5}=\frac{y+4}{7}=\frac{2 z-6}{4}
$$

Write the vector equation for the line.

## SECTION - B

Q.11. If the function $f: R \rightarrow R$ be given by $f(x)=x^{2}+2$ and $g: R \rightarrow R$ be given by

$$
g(x)=\frac{x}{x-1}, x \neq 1
$$

find $\boldsymbol{f o g}$ and $\boldsymbol{g o f}$ and hence find $\boldsymbol{f o g}(2)$ and $\boldsymbol{g o f}(-3)$. 4. marks
Q.12. Prove that:

$$
\tan ^{-1}\left[\frac{\sqrt{1+x}-\sqrt{1-x}}{\sqrt{1+x}+\sqrt{1-x}}\right]=\frac{\pi}{4}-\frac{1}{2} \cos ^{-1} x, \frac{-1}{\sqrt{2}} \leq x \leq 1 .
$$

OR
If

$$
\tan ^{-1}\left(\frac{x-2}{x-4}\right)+\tan ^{-1}\left(\frac{x+2}{x+4}\right)=\frac{\pi}{4}, \text { find the value of } x \text {. }
$$

Q.13. Using properties of determinants, prove that: 4 marks

$$
\left|\begin{array}{ccc}
x+y & x & x \\
5 x+4 y & 4 x & x \\
10 x+8 y & 8 x & 3 x
\end{array}\right|=x^{3}
$$

Q.14. Find the value of

$$
\frac{d y}{d x} \text { at } \theta=\frac{\pi}{4},
$$

$$
\text { if } \boldsymbol{x}=\boldsymbol{a} \boldsymbol{e}^{\boldsymbol{\theta}}(\sin \boldsymbol{\theta}-\cos \boldsymbol{\theta}) \text { and } \boldsymbol{y}=\boldsymbol{a} \boldsymbol{e}^{\boldsymbol{\theta}}(\boldsymbol{\operatorname { s i n }} \boldsymbol{\theta}+\boldsymbol{\operatorname { c o s } \boldsymbol { \theta }}) .4 \text { marks }
$$

Q.15. If $y=P e^{a x}+Q e^{b x}$, show that: $\qquad$

$$
\frac{d^{2} y}{d x^{2}}-(a+b) \frac{d y}{d x}+a b y=0
$$

Q.16. Find the value(s) of $x$ for which $y=[x(x-2)]^{2}$ is an increasing function.

## OR

Find the equations of the tangent and normal to the curve

$$
\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=1 \text { at the point }(\sqrt{2} a, b) .
$$

Q. 17. Evaluate:

$$
\int_{0}^{\pi} \frac{4 x \sin x}{1+\cos ^{2} x} d x
$$

## OR

$$
\text { Evaluate: } \int \frac{x+2}{\sqrt{x^{2}+5 x}+6} d x
$$

Q. 18. Find the particular solution of the differential equation $\frac{d y}{d x}=1+x+y+x y$,

$$
\text { given that } y=0 \text { when } x=1
$$

Q. 19. Solve the differential equation 4 marks

$$
\left(1+x^{2}\right) \frac{d y}{d x}+y=e^{\tan ^{-1} x}
$$

Q. 20. Show that the four points $A, B, C$ and $D$ with position vectors

$$
4 \hat{\imath}+5 \hat{\jmath}+\widehat{k},-\hat{\jmath}-\widehat{k}, 3 \hat{\imath}+9 \hat{\jmath}+4 \widehat{k} \text { and } 4(-\hat{\imath}+\hat{\jmath}+
$$

$\widehat{\boldsymbol{k}}$ )respectively are coplanar.
OR
The scalar product of the vector $\overrightarrow{\boldsymbol{a}}=\hat{\boldsymbol{\imath}}+\hat{\boldsymbol{\jmath}}+\widehat{\boldsymbol{k}}$ with a unit vector along the sum of vectors

$$
\vec{b}=2 \hat{\imath}+4 \hat{\jmath}-5 \widehat{k} \text { and } \vec{c}=\lambda \hat{\imath}+2 \hat{\jmath}+3 \widehat{k} \text { is equal to one } .
$$

find the velue of $\lambda$ and hence find the unit vector along $\vec{b}+\vec{c}$.
Q. 21. A line passes through $(2,-1,3)$ and is perpendicular to the lines

$$
\begin{aligned}
& \overrightarrow{\boldsymbol{r}}=(\hat{\imath}+\hat{\jmath}-\widehat{\boldsymbol{k}})+\lambda(2 \hat{\imath}+2 \hat{\jmath}-\widehat{\boldsymbol{k}}) \text { and } \\
& \overrightarrow{\boldsymbol{r}}=(2 \hat{\imath}-\hat{\boldsymbol{\jmath}}-3 \widehat{\boldsymbol{k}})+\mu(\hat{\imath}+2 \hat{\jmath}-2 \widehat{\boldsymbol{k}}) .
\end{aligned}
$$

Obtain its equation in vector and Cartesian form.
4 marks
Q. 22. An experiment succeeds thrice as often as it fails. Find the probability that in the next five trails, there will be at least 3 successes.

SECTION- C
Question numbers $230 \% 29$ carry 6 marks each.
Q. 23. Two school A and B want to award their selected students on the values of sincerity, truthfulness and helpfulness. The school A wants to award Rs $x$ each, Rs $y$ each and Rs $z$ each for the three respective values to 3,2 and 1 student respectively with a total award money of Rs 1,600.School $B$ wants to spend rs 2,300 to award its 4,1 and 3student on the respective values ( by giving the same award money to the three values as before). If the total amount of award for one prize on each value is rs 900 , using matrices, find the award money for each value. A part from these three values, suggest one more value which should be considered for award. 6 marks
Q.24. Show that the altitude of the right circular cone of maximum volume that can be inscribed in a sphere of radius $r$ is $\frac{4 r}{3}$. Also show that the maximum volume of the cone $\frac{8}{27}$ of the volume of the sphre. 6 marks?
Q.25. Evaluate: 6 marks

$$
\int \frac{1}{\cos ^{4} x+\sin ^{4} x} d x
$$

Q26. Using integration, find the area of the region bounded by the triangle whose vertices are $(-1,2),(1,5)$ and $(3,4) .6$ marks
Q.27. Find the equation of the plane through the line of intersection of the planes $x+y+$ $z=1$ and $2 x+3 y+4 z=5$ which is perpendicular to the plane $x+y+z=0$. Also find the distance of the plane obtained above from the origin. 6 markes

OR
Find the distance point $(2,12,5)$ from the point of intersection of the line
$\vec{r}=\mathbf{2} \hat{\imath}-4 \hat{\jmath}+2 \widehat{k}+\lambda(3 \hat{\imath}+4 \hat{\jmath}+2 \widehat{k})$ and the plane

$$
\overrightarrow{\boldsymbol{r}} \cdot(\hat{\boldsymbol{\imath}}-\mathbf{2} \hat{\boldsymbol{\jmath}}+\widehat{\boldsymbol{k}}=\mathbf{0} .
$$

Q.28. A manufacturing company makes two types of teaching aids $A$ and $B$ of Mathematics for class XII. Each of A requires 9 labour hours of fabricating and 1 labour hour for finishing. Each type of $B$ requires 12 labour hours for fabricating and 3 labour hours finishing. for and finishing the maximum labour hours available per week are 180 and 30 respectively. The company makes a profit of Rs80 on each piece of type A and Rs120 on each piece of type B. How many pieces of type A type B Should be manufactured per week to get a maximum profit? Make it as an LPP and solve graphically. What is the maximum profit per week?
Q.29. There are three coins. One is a two - headed coin (having head on both faces ), another is a biased coin that comes up heads $75 \%$ of the times and third is also a biased coin that comes up tails $40 \%$ of the times. one of the three coin is chosen at random and tossed, and it shows head. What the two - headed coin?

## OR

Two numbers are selected at random (without replacement) from the first six positive integers. Let $X$ denote the larger of the two numbers obtained. Find the probability distribution of the random variable $X$, and hence find the mean of the distribution.

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