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CBSE 12th Mathematics 2013 Unsolved Paper

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CBSE 12th Mathematics 2013 Unsolved Paper Outside Delhi

TIME - 3HR. | QUESTIONS - 29

THE MARKS ARE MENTIONED ON EACH QUESTION

SECTION – A

Question numbers 1 to 10 carry 1 mark each.

Q.1. write the principal value of

$$\tan^{-1}(\sqrt{3}) - \cot^{-1}(-\sqrt{3}).\ \textit{1 mark}$$

Q.2. Write the value of

$$\tan^{-1}\left[\left(2\sin^{-1}\frac{\sqrt{3}}{2}\right)\right].\quad \textit{1 mark}$$

Q.3. for what value of x, is the matrix *1 mark*

$$A = \begin{bmatrix} 0 & 1 & -2 \\ -1 & 0 & 3 \\ x & -3 & 0 \end{bmatrix} \textbf{a skew} - \textbf{symmetric matrix ?}$$

Q.4. if matrix $A = \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix}$ and $A^2 = KA$, I then write the value of k. *1 mark*

Q.5. Write the differential equation representing the family of curves $y = mx$ when m is an arbitrary consent. *1 mark*

Q.6. if A_{ij} is the cofactor of the a_{ij} of the determinant. *1 mark*

$$\begin{vmatrix} 2 & -3 & 5 \\ 6 & 0 & 4 \\ 1 & 5 & -7 \end{vmatrix} \textbf{the value of } a_{32}.A_{32}.$$

Q.7. P and Q are two points with position vectors $3\vec{a} - 2\vec{b}$ and $\vec{a} + \vec{b}$ respectively. Write the position vector of a point R which divides the line segment PQ in the ratio 2 : 1 externally. *1 mark*

Q.8. Find $|\vec{x}|$, if for a unit vector $\vec{a}$, $(\vec{x} - \vec{a}).(\vec{x} + \vec{a}) = 15$. *1 mark*

Q.9. Find the length of the perpendicular drawn from the origin to the plane

$$2x - 3y + 6z + 21 = 0.\ \textit{1 mark}$$

Q.10. The money to be spent for the welfare of the employees of a firm is proportional to the rate of change of its total revenue (marginal revenue). If the total revenue (in rupees) received from the sale of x units of a product is given by

$R(x) = 3x^2 + 36x + 5$, **find the marginal revenue, when $x = 5$, and write which value does the question indicate.** *1 mark*

SECTION – B

Question numbers 11 to 22 carry 4 marks each

Q.11. Consider $f: R_+ \to [4, \infty)$ given by $f(x) = x^2 + 4$. Show that f is invertible with the inverse f^{-1} of f given by $f^{-1}(y) = \sqrt{y-4}$ where R_+ is the set of all non – negative real numbers. *4 marks*

Q.12. Show that: *4 marks*

$$tan\left(\frac{1}{2}sin^{-1}\frac{3}{4}\right) = \frac{4-\sqrt{7}}{3}$$

OR

Solve the following equation: *4 marks*

$$cos\left(tan^{-1}x\right) = sin\left(cot^{-1}\frac{3}{4}\right).$$

Q.13. Using properties of determinants, prove the following: *4 marks*

$$\begin{vmatrix} x & x+y & x+2y \\ x+2y & x & x+y \\ x+y & x+2y & x \end{vmatrix} = 9y^2(x+y).$$

Q.14. if $y^x = e^{y-x}$, prove that *4 marks*

$$\frac{dy}{dx} = \frac{(1+log\ y)^2}{log\ y}.$$

Q.15. Differentiate the following with respect to x: *4 marks*

$$sin^{-1}\left(\frac{2^{x+1}.3^x}{1+(36)^x}\right)$$

Q.16. Find the value of k, for which

$$f(x)\begin{cases} \dfrac{\sqrt{1+kx}-\sqrt{1-kx}}{x} &, if -1 \le x < 0 \\ \dfrac{2x+1}{x-1} & if\ 0 \le x < 1 \end{cases}$$

Is continuous at x = 0. *4 marks*

OR

If $x\, a\, \cos^3 \theta$ and $y = a\, \sin^3 \theta,$ then find the value of $\dfrac{d^2 y}{dx^2}$ at $\theta, = \dfrac{\pi}{6}.$

Q.17. Evaluate: *4 marks*

$$\int \frac{\cos 2x - \cos 2 \propto}{\cos x - \cos \propto}\, dx$$

OR

Evaluate:

$$\int \frac{x+2}{\sqrt{x^2 + 2x + 3}}\, dx.$$

Q.18. Evaluate: *4 marks*

$$\int \frac{dx}{x(x^5 + 3)}.$$

Q.19. Evaluate: *4 marks*

$$\int_{0}^{2\pi} \frac{1}{1 + e^{\sin x}}\, dx.$$

Q.20. *If $\vec{a} = \hat{\imath} - \hat{\jmath} + 2\hat{k}$ and $\vec{b} = 5\hat{\imath} - \hat{\jmath} + \lambda\hat{k},$ then find the value of $\lambda.$ so that $\vec{a} + \vec{b}$ and*

    $\vec{a} - \vec{b}$ are perpendicular vectors. *4 marks*

Q.21. Show that the lines

$$\vec{r} = 3\hat{\imath} + 2\hat{\jmath} - 4\hat{k} + \lambda(\hat{\imath} + 2\hat{\jmath} + 2\hat{k});$$

$$\vec{r} = 5\hat{\imath} - 2\hat{\jmath} + \mu(3\hat{\imath} + 2\hat{\jmath} + 6\hat{k})$$

    Are intersection. Hence find their point of intersection. *4 marks*

OR

    Find the vector equation of the plane through the points (2, 1, -1) and (-1,3,4) and

    Perpendicular to the plane $x - 2y + 4z = 10$.

Q. 22. The probabilities of two student's A and B coming to the school in time are

    $\dfrac{3}{7}$ *and* $\dfrac{5}{7}$ **respectively. Assuming that the events, 'A coming in time' and 'B coming in time' are independent, find the probability of only one of them coming to the school in time.**

    Write at least one advantage of coming to school in time. *4 marks*

SECTION- C

Question numbers 23 to 29 carry 6 marks each

Q. 23. Find the area of the greatest rectangle that can be inscribed in an ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1.$$ *6 marks*

OR

Find the equation of tangents to the curve $3x^2 - y^2 = 8$, which pass through the

point $\left(\frac{4}{3}, 0\right)$.

Q. 24. Find the area of the region bounded by the parabola   *6 marks*

$$y = x^2 \ and \ y = |x|.$$

Q.25. Find the particular solution of the differential equation   *6 marks*

$$(tan^{-1}y - x)dy = (1 + y^2)dx, given \ that$$

$$When \ x = 0, y = 0.$$

Q. 26. Find the equation of the plane passing through the line of intersection of the

Planes $\vec{r}.(\hat{\imath} + 3\hat{\jmath}) - 6 = 0 \ and$

$$\vec{r}.(3\hat{\imath} - \hat{\jmath} - 4\hat{k}) = 0, whose$$

Perpendicular distance from origin is unity.   *6 marks*

OR

Find the vector equation of the line passing through the point (1, 2, 3) and parallel to the planes

$$\vec{r}.(\hat{\imath} - \hat{\jmath} + 2\hat{k}) = 5$$

$$and \quad \vec{r}.(3\hat{\imath} + \hat{\jmath} + \hat{k}) = 6.$$

Q. 27. In a hockey match, both teams A and B scored same number of goals up to the end of the game, so to decide the winner, the referee asked both the captains to throw a die alternately and decided that the team, whose captain gets a six first, will be declared the winner. If the captain of team A was asked to start, find their respective probabilities of winning the match and state whether the decision of the referee was fair or not.   *6 marks*

Q. 28. A manufacturer considers that men and women workers are equally efficient and so he pays them at the same rate. He has 30 and 17 units of workers (male and female) and capital respectively; which he uses to produce two types of goods A and B. to produce one unit of A, 2 workers and 3 units of capital are required while 3 workers and 1 unit of capital is required to produce one unit of B. if A and B are priced at Rs100 and Rs120 per unit respectively, how should he use his resources to maximize the total revenue? Form the above as an LPP and solve graphically.
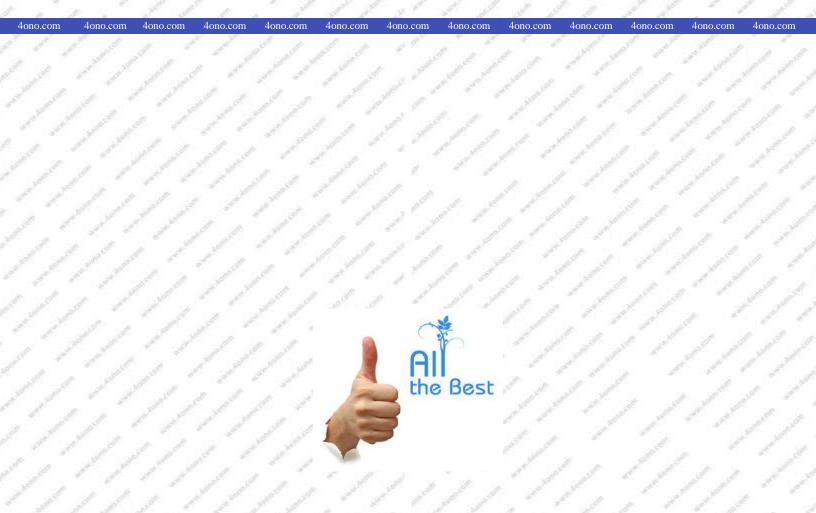
Do you agree with this view of the manufacturer that men and women workers are equally efficient and so should be paid at the same rate? *6 marks*

Q. 29. The management committee of a residential colony decided to award some of its members (say x) for honesty, some (say y) for helping other (say z) for supervising the workers to keep the colony neat and clean. The sum of all the awardees is 12. Three times the sum of awardees for cooperation and supervision added to two times the number of awardees for honesty is 33. If the sum of the number of awardees for honesty and supervision is twice the number of awardees for helping others, using matrix method, find the number of awardees of each category. Apart from these values, namely, honesty, cooperation and supervision, suggest one more value which the management of the colony must include for awards. *6 marks*

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