## SECTION A

Question numbers 1 to 10 carry 3 marks each.
Q. 1. Express the following as a rational expression in lowest terms:
$\frac{x^{2}-8}{x^{2}-4} \times \frac{x^{2}+6 x+8}{x^{2}-2 x+1} \div \frac{x^{2}+2 x+4}{x^{2}+2 x-3}$
Ans: $\frac{x^{2}+7 x+12}{x-1}$
Q. 2. Find 10 th term from end of the A.P. 4, 9, 14,.. 254.

Ans:(209)
Q. 3. Solve the following system of linear equations:
$a x+b y=a-b$
$b x-a y=a+b$
Ans: $(x=1, y=-1)$
Q. 4. Find the L.C.M. of the following polynomials:
$2 x^{3}-128 ; x^{2}-9 x+20 ; x^{2}-16$
Ans: $\left\lfloor 2(x-4)\left(x+4(x-5)\left(x^{2}+4 x+16\right)\right\rfloor\right.$
Q. 5. Solve for x .
$\frac{1}{a+b+x}=\frac{1}{a}+\frac{1}{b}+\frac{1}{x} ; a \neq 0, b \neq 0, x \neq 0$
Ans:(c/a,-b/a)
Or
Solve for x .
$a b x^{2}+\left(b^{2}-a c\right) x-b c=0$
Ans:(c/a,-b/a)
Q. 6. Find the number of terms of the A.P. $54,51,48$... so that their sum is 513.

Ans:( $\mathrm{n}=18$ or $\mathrm{n}=19$ )
Or
If the $n$th term of an A.P. is $(2 n+1)$, find the sum of first $n$ terms of the A.P.

## Ans:n (n+2)

Q. 7. A loan of Rs 10,815 is to be returned in three equal half-yearly installments.

Calculate the amount of each installment, if the rate of interest is $\quad \frac{13 \frac{1}{3} \%}{}$ per annum, compounded half-yearly.

## Ans:(Rs. 4,096)

Q. 8. A fan is available for Rs 970 cash or Rs 210 as cash down payment followed by three equal monthly installments of Rs 260 each. Find the rate of interest charged under installments plan.

## Ans:(16\% p.a.)

Q. 9. In the figure, $\triangle A B C$ and $\triangle D B C$ are on the same base $B C$. $A D$ and $B C$ intersect
at O. prove that $\frac{\operatorname{area}(\triangle A B C)}{\operatorname{area}(\triangle D B C)}=\frac{A O}{D O}$

Q. 10. OD is perpendicular to a chord $A B$ of a circle whose centre is $O$. If $B C$ is a diameter, prove that CA $=20 \mathrm{D}$.

## SECTION B

## Question numbers 11 to 20 carry 4 marks each.

Q. 11. Solve the following system of equations graphically:
$x+2 y=5 \quad 2 x-3 y=-4$
Also find the points where the lines meet the x -axis.

## Ans: $B(5,0), C(-2,0)$

Q. 12. The sum of two numbers $a$ and $b$ is 15 , and the sum of their reciprocals $1 / a$ and $1 / b$ is $3 / 10$. Find the numbers $a$ and $b$.

Ans: $(a=10, b=5$ or $a=5, b=10)$
Q. 13. A hemispherical bowl of internal radius 9 cm is full of liquid. The liquid is to be filled into cylindrical shaped small bottles each of diameter 3 cm and height 4 cm . How many bottles are needed to empty the bowl?

## Ans:(54)

Q. 14 Prove that:
$\tan ^{2} A-\tan ^{2} B=\frac{\sin ^{2} A-\sin B}{\cos ^{2} A-\cos ^{2} B}$
find the value of:
$\frac{-\tan \theta \cdot \cot \left(90^{\circ}-\theta\right)+\sec \theta \cdot \operatorname{cosec}\left(90^{\circ}-\theta\right)+\sin ^{2} 35^{\circ}+\sin ^{2} 55^{\circ}}{\tan 10^{\circ} \tan 20^{\circ} \tan 30^{\circ} \tan 70^{\circ} \tan 80^{\circ}}$
Ans: ${ }^{(2 \sqrt{3}}$
Q. 15. Draw a circle of radius 3.5 cm . From a point $P$ outside the circle at a distance of 6 cm from the centre of circle, draw two tangents to the circle.
Q. 16. Find the value of $x$ such that $P Q=Q R$ where the coordinates of $P, Q$ and $R$ are $(6,-1)$;
$(1,3)$ and $(x, 8)$ respectively.
Ans: $(x=5$ or $x=-3)$
Or
Find a point on x -axis which is equidistant from the points $(7,6)$ and $(-3,4)$.

## Ans:(3,0)

Q. 17. The line-segment joining the points $(3,-4)$ and $(1,2)$ is trisected at the points $P$ and $Q$. If the Coordinates of $P$ and $Q$ are $(p,-2)$ and $\left(\frac{5}{3}, q\right)$ respectively, find the values of $p$ and $q$.

Ans:(p=7/3; q=0)
Q. 18. Find the mean of the following distribution:

| Class | Number of Students |
| :---: | :---: |
| $4-8$ | 2 |
| $8-12$ | 12 |
| $12-16$ | 15 |
| $16-20$ | 25 |
| $20-24$ | 18 |
| $24-28$ | 12 |
| $28-32$ | 13 |
| $32-36$ | 3 |

## Ans:(19-92)

Q. 19. Given below is the expenditure of a person on different items out of his salary of Rs 14,400 .

| Item: | Clothing | Food | Rent | education | others | G. total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Expn. : (in <br> Rs.) | 2,800 | 3,600 | 3,600 | 1,800 | 2,600 | 14,400 |

Draw a pie-chart to depict the above data.
Q. 20. A card is drawn at random from a well shuffled pack of 52 cards. Find the Probability that the card drawn is neither a red card nor a queen.

Ans:(6/13)

## SECTION C

## Question numbers 21 to 25 carry 6 marks each.

Q. 21. Prove that in a right angled triangle the square on the hypotenuse is equal to the sum of the squares on other two sides.

Using the above result, prove that the sum of squares on the sides of a rhombus is equal to sum of squares on its diagonals.
Q. 22. On a horizontal plane there is a vertical tower with a flag pole on the top of the tower. At a point 9 metres away from the foot of the tower the angle of elevation of the top and bottom of the flag pole are $60^{\circ}$ and $30^{\circ}$ respectively. Find the height of the tower and flag pole mounted on it.

Ans: ( $\mathbf{5 . 1 9} \mathbf{~ m , ~ 1 0 . 3 8 m}$ )

Or
From a building 60 metres high the angles of depression of the top and bottom of a lamppost are $30^{\circ}$ and $60^{\circ}$ respectively. Find the distance between the lamppost and building. Also find the difference of height between building and lamppost.

## Ans:(34.6 m, 20m)

Q. 23. A tent is in the shape of a right circular cylinder up to a height of 3 m and conical above it. The total height of the tent is $13-5 \mathrm{~m}$ and radius of base is 14 m . Find the cost of cloth required to make the tent at the rate of Rs 80 per sq. m .

## Ans; (Rs 82,720)

Or

The radii of circular ends of a solid frustum of a cone are 33 cm and 27 cm and its slant height is 10 cm . Find its total surface area.

## Ans:(7599-43 cm2)

Q. 24. If a line touches a circle and from the point of contact a chord is drawn, prove that the angles which this chord makes with the given line are equal respectively to the angles formed in the corresponding alternate segments.


Using the above theorem, prove the following: $P$ is mid point of arc APB. Prove that tangent $Q R$ drawn at $P$ to the circle is parallel to $A B$.
Q. 25. The monthly income of Ruchi (age 30 years) is Rs. 18,200 (excluding HRA). She donates Rs. 8,400 towards Prime Minister Relief Fund (Relief 100\%) and Rs. 12,000 to an orphanage (Relief 50\%). She contributes Rs. 4,500 per month towards Provident Fund and Rs. 2,500 per quarter as LIC premium. She purchases National Saving Certificates worth Rs. 8,000. She pays Rs. 900 per month as income-tax for the first 11 months. Calculate her income-tax liability for last month of the year.

For calculating income tax, use the following:
(a) Standard Deduction :
(i) Rs. 30,000 if incomes is up to Rs.5,00,000
(ii)Rs. 20,000 if income is more than Rs.5,00,000
(b) Rates of income tax:

## Income tax

$10 \%$ of the amount exceeding Rs. 50,000
Rs.1,000+20\% of the amount exceeding Rs. 60,000
Rs. 19, 000+30\% of the amount exceeding Rs.1,50,000
(i) $20 \%$ of the savings subject to a maximum of Rs. 14,000 if the gross incomes is upto Rs.1,50,000.
(ii) $15 \%$ of the savings subject to a maximum is upto

Rs. 10,500 if the gross income is between Rs. $1,50,001$ to
$2 \%$ of the income tax payable
For female, maximum Rs. 5,000 over and above the rebate

## Slab <br> Slab

(i) Upto Rs.50,000
(ii) From Rs.50,001 to Rs. 60,000
(iii)From Rs.60,001 to Rs. 1,50,000
(iv) Above Rs.1,50,000
(c) Rebate in tax
(d) Educational cess
(e) Special Rebate
(Ans;Rs. 1,014)
(c) Rebate in

No tax Rs.5,00,000.

For female,
on savings.

